

# An Accurate, but Novel Application of the Relative Flow Technique, Using a Moveable Aperture Source of Gas Atoms to Measure Elastic Electron Scattering Differential Cross Sections.

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# Contents

- Basic electron scattering
  - Experimental setup
  - Basic scattering equation
- Variations employed in our experiment
  - Moveable, collimated gas source
  - Thin aperture gas source
- Relative flow technique
  - Basic equations
  - Experimental verification of principle
  - Flow rate measurements
- Differential cross sections for Ethylene ( $C_2H_4$ )
  - Incident energies of 2eV, 5eV, 10eV, 20eV, 30eV
- Conclusions

# Basic Layout

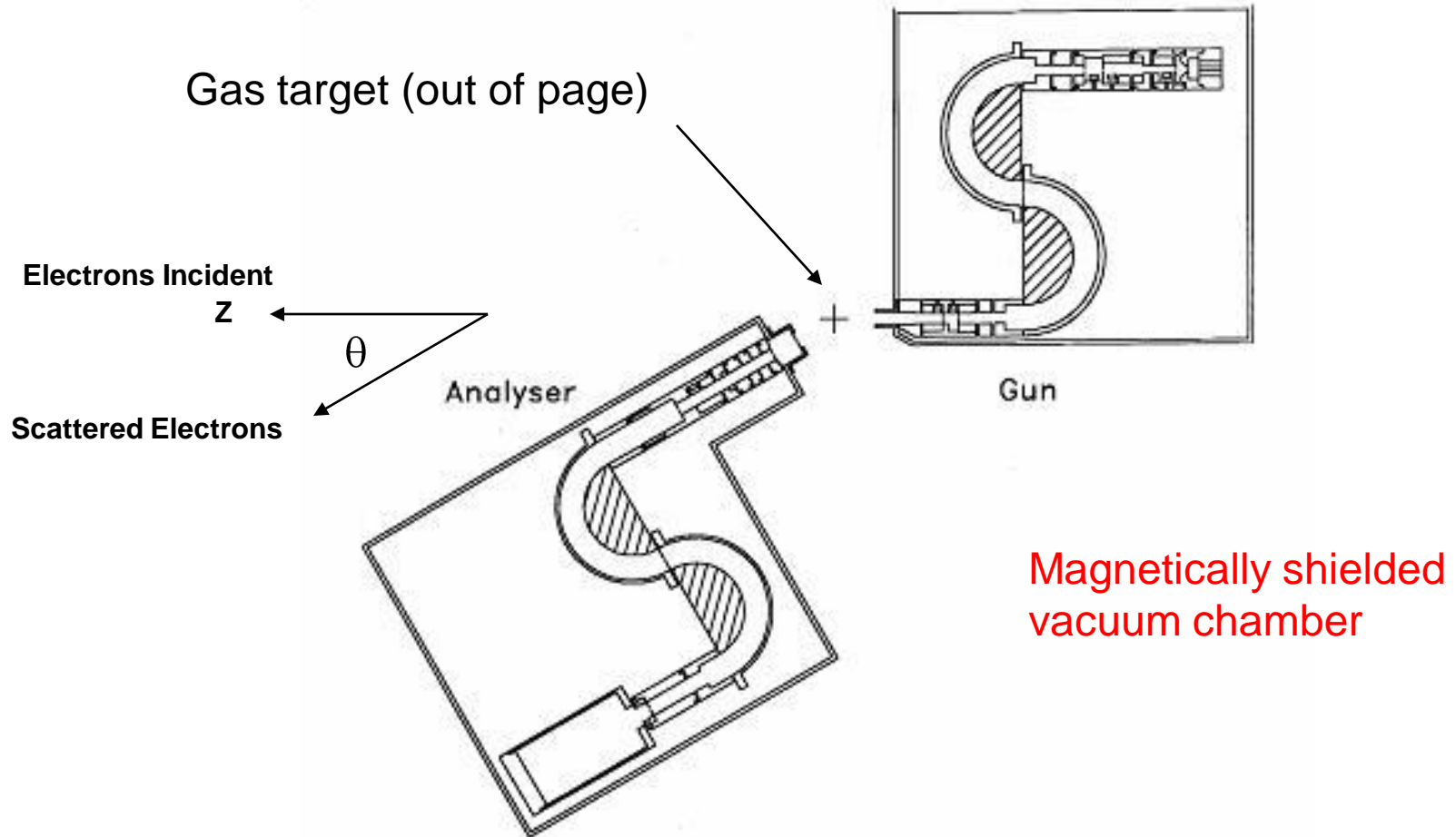
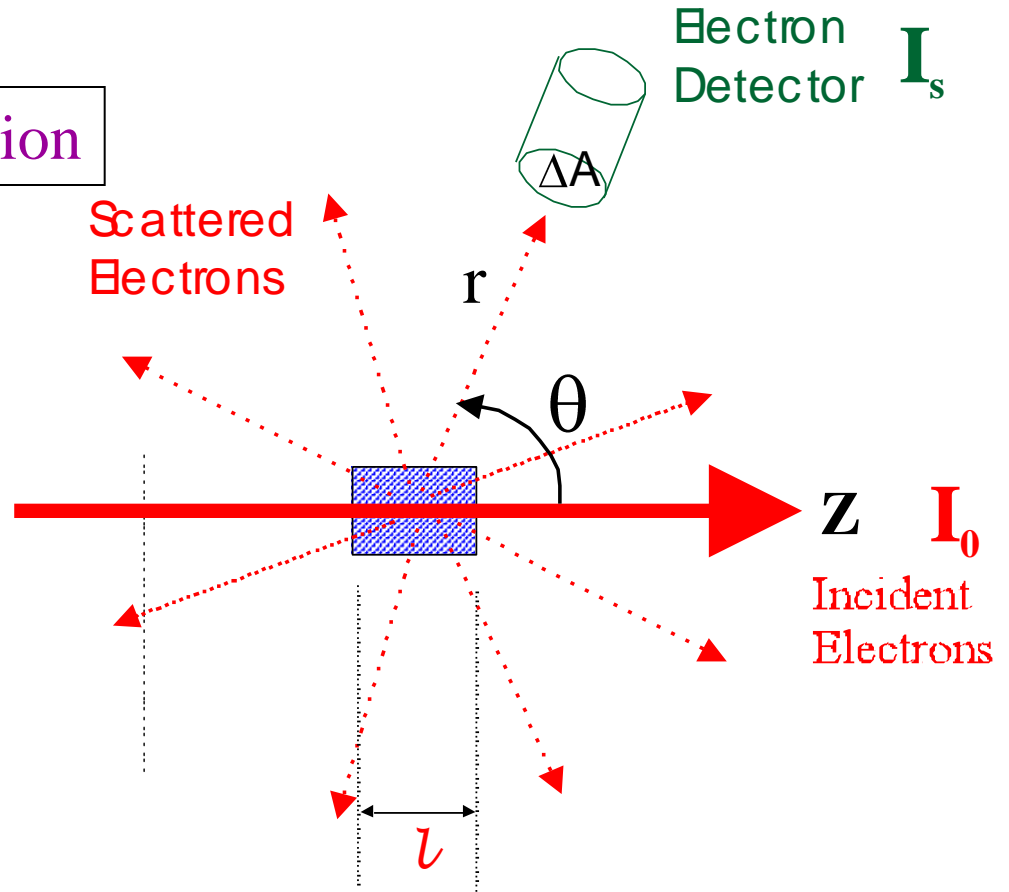


Diagram of our electron spectrometer

# The Differential Cross Section

$$d\sigma/d\Omega (\theta)$$



## Schematics of Experimental Setup

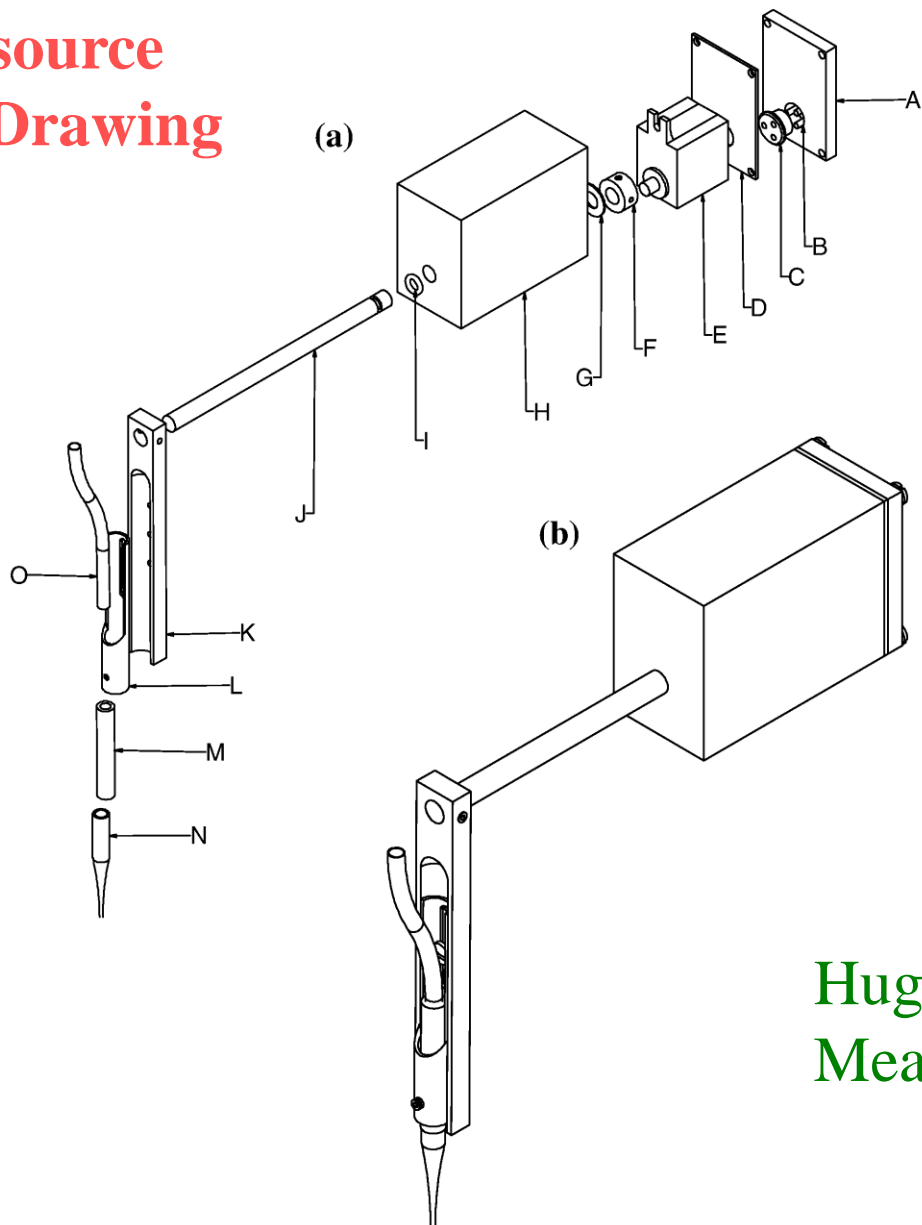
$$\Delta\Omega = \frac{\Delta A}{r^2}$$

$$I_s = I_0 n l \frac{d\sigma}{d\Omega} \Delta\Omega$$

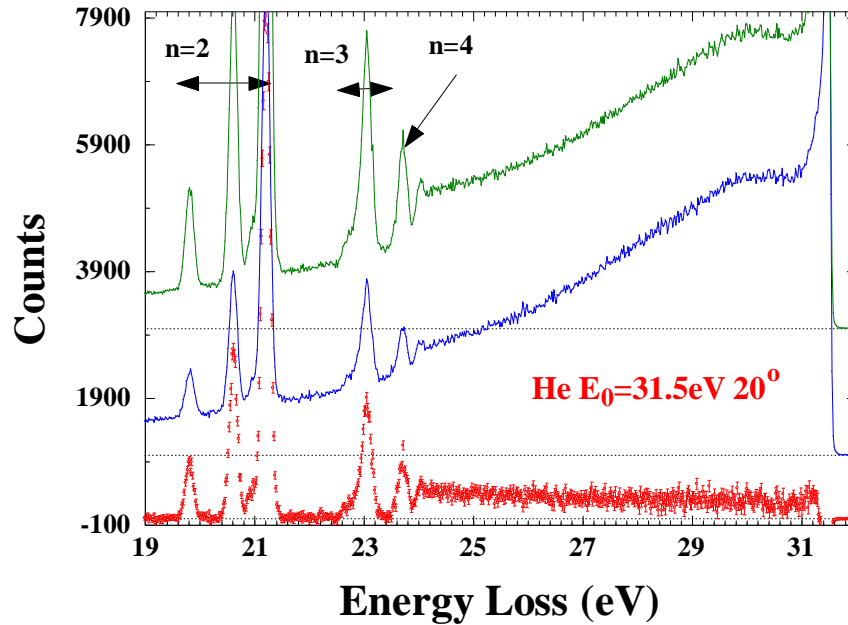
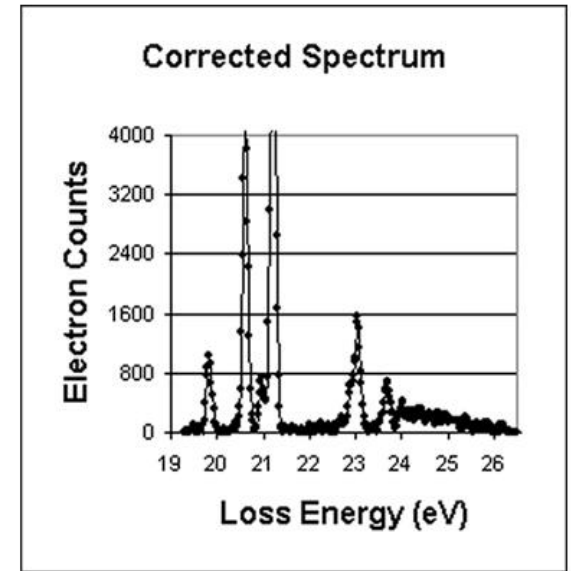
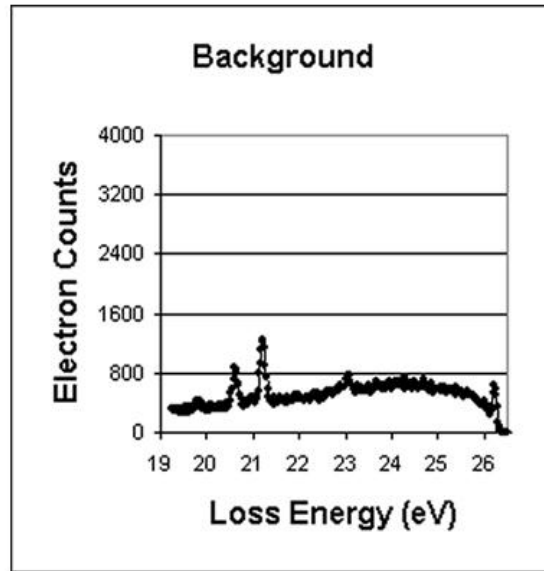
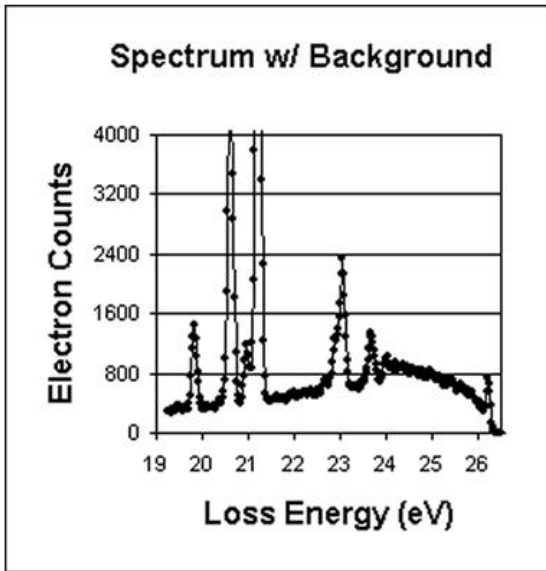
Units:  $I_0$  ( $s^{-1}$ ),  $I_s$  ( $s^{-1}$ ),  $n$  ( $cm^{-3}$ ),  $l$  (cm)

$d\sigma/d\Omega (\theta)$  ( $cm^2/sr$ )

# Moveable source Assembly Drawing



Hughes *et al.* 2003  
Meas. Sci. & Tech.



**Helium**  
Schow et al.  
2005, CSUF.

# Relative Flow Method

Flow standard gas (He)

Measure scattered signal

Flow gas X with the same gas distribution

Determine DCS for X:

$$\text{DCS}_X(E_0, \theta) = \text{DCS}_{\text{He}}(E_0, \theta) \frac{\text{RFR}_{\text{He}}}{\text{RFR}_X} \frac{I_{S_X}}{I_{S_{\text{He}}}} \sqrt{\frac{M_{\text{He}}}{M_X}}$$

# Mean Free Path Issue

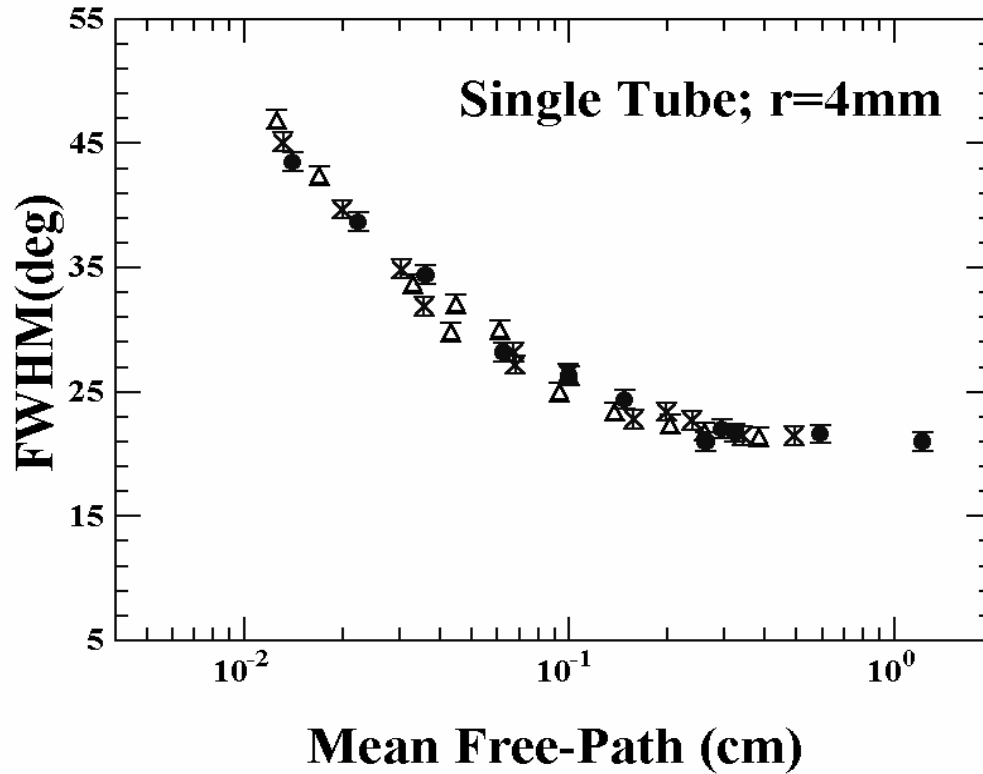
$$\lambda = \frac{1}{\sqrt{2}\pi n\delta^2}$$

$\delta$  is the Gas Kinetic Molecular Diameter

- Olander and Kruger (1970) – Angular profile (FWHM) of gases for tubes dependent on the mean-free path.
- Rugamas et al. (2000) Experimental evidence

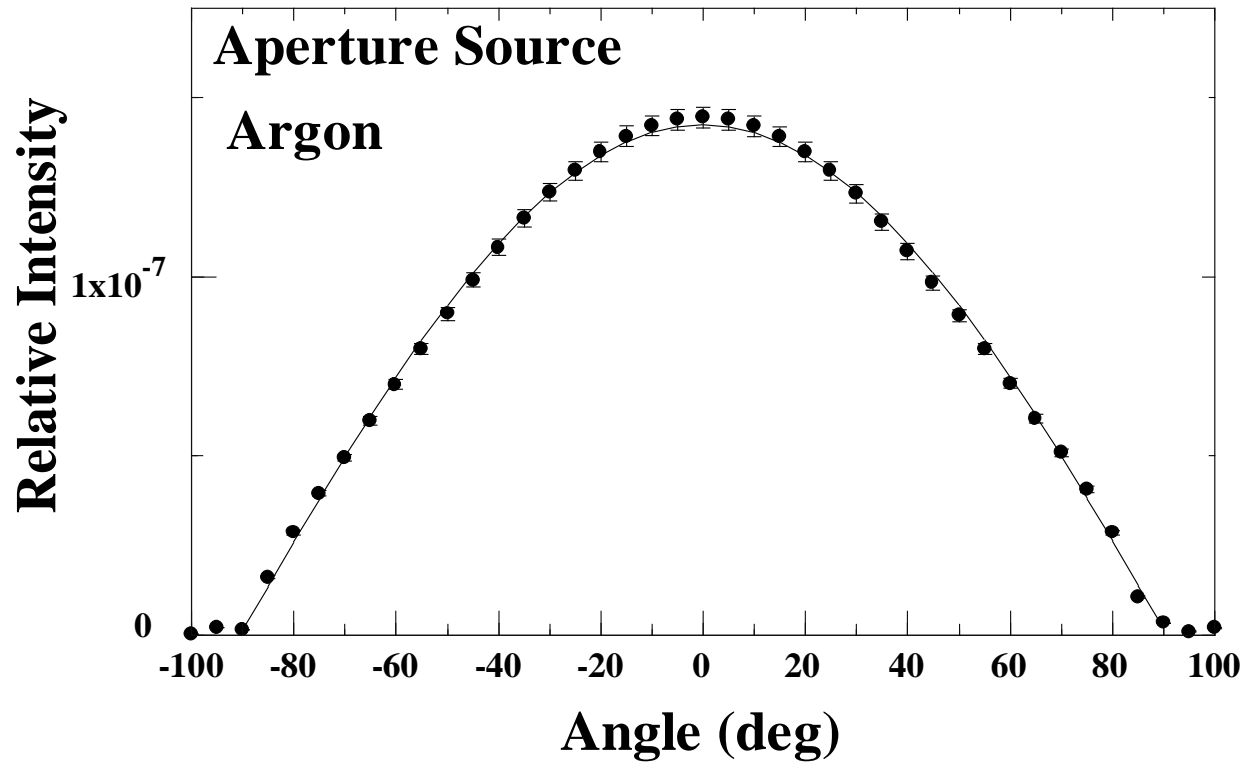


# Profiles vs. Mean-Free Path



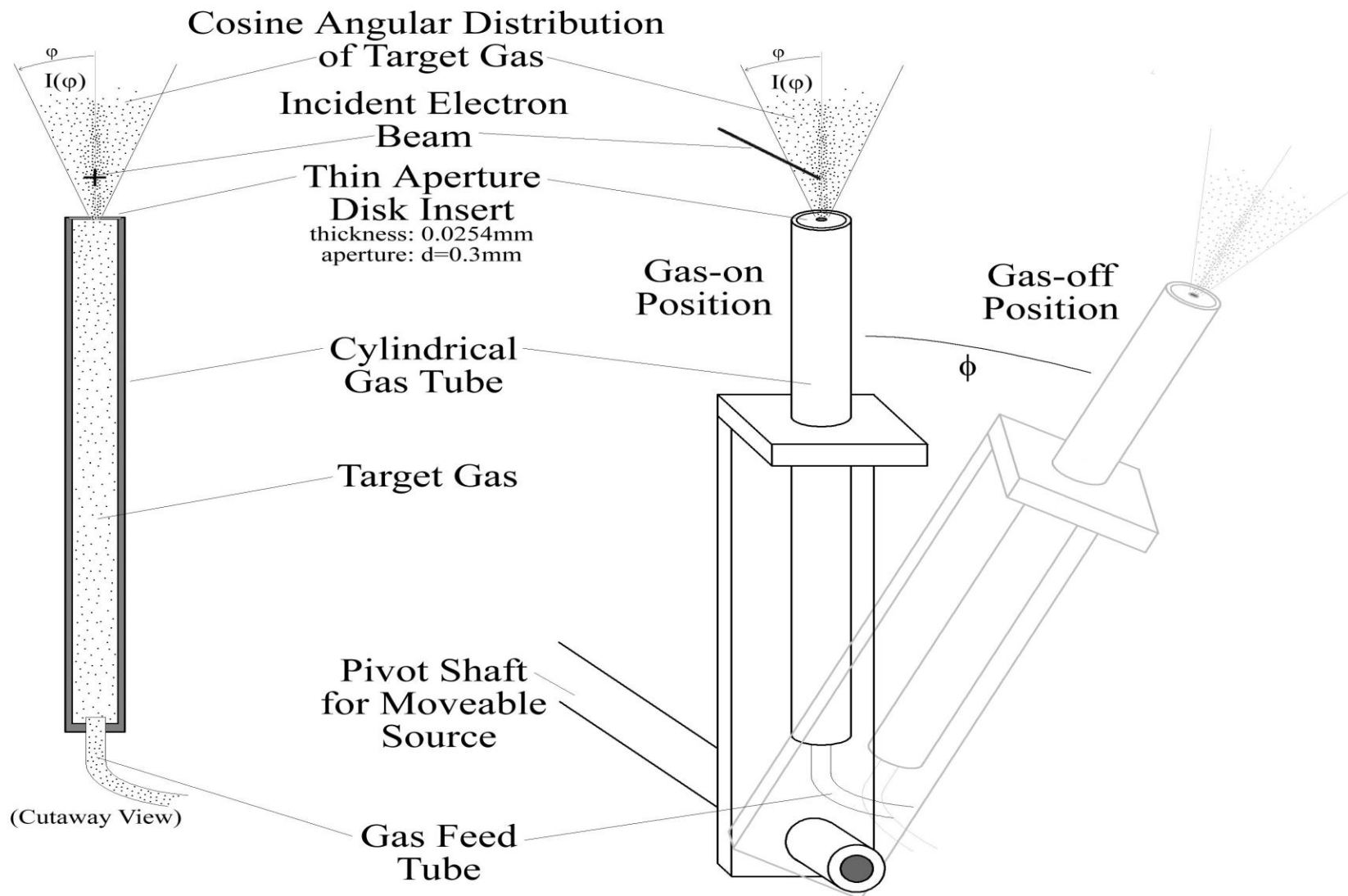
Rugamas et al. (2000)

# Gas Distribution of a Thin Aperture Source



Rugamas et al. (2000) CSUF

# Thin-Aperture Moveable Gas Source



# Transformation of Basic Scattering Equation

$$I_s = I_o n \frac{d\sigma}{d\Omega} \Delta\Omega \quad \text{Basic scattering amplitude from theory}$$

Flow rate

RMS velocity

Ideal Gas Law

$$\dot{N} = n A v$$

$$\frac{1}{2} m v^2 = \frac{3}{2} k T$$

$$P V = N k T$$

$$n = \frac{\dot{N}}{A v}$$

$$v = \sqrt{\frac{3 k T}{m}}$$

$$\dot{P} = \frac{d}{dt} \left( \frac{N k T}{V} \right)$$

$$n = \frac{\dot{N} \sqrt{m}}{A \sqrt{3 k T}}$$

$$\dot{P} = \frac{k}{V} (N \dot{T} + \dot{N} T)$$

$$\alpha = \frac{1}{A \sqrt{3 k T}}$$

$$\dot{P} = \frac{k T}{V} \dot{N}$$

$$n = \alpha \dot{N} \sqrt{m}$$

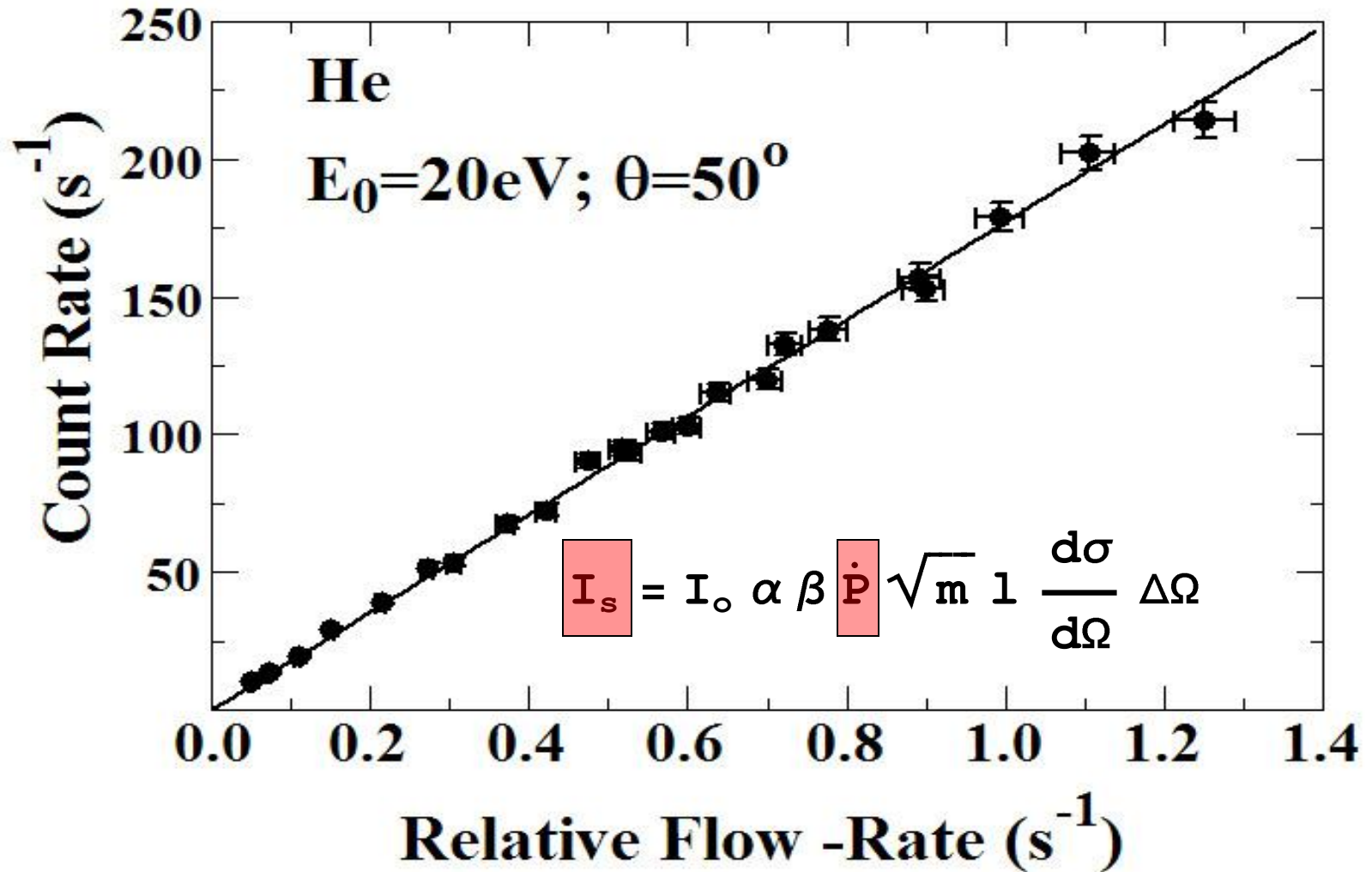
$$\beta = \frac{V}{k T}$$

$$\dot{N} = \beta \dot{P}$$

$$I_s = I_o \alpha \beta \dot{P} \sqrt{m} \frac{d\sigma}{d\Omega} \Delta\Omega$$

New scattering equation

# Experimental Verification



# Differential Cross Section of Gas X

$$I_s^x = I_o^x \alpha_x \beta_x \dot{P}_x \sqrt{m_x} l_x \frac{d\sigma_x}{d\Omega} \Delta\Omega_x$$

$$I_s^{He} = I_o^{He} \alpha_{He} \beta_{He} \dot{P}_{He} \sqrt{m_{He}} l_{He} \frac{d\sigma_{He}}{d\Omega} \Delta\Omega_{He}$$

$$l_x = l_{He}$$

Same distribution of gas

$$\alpha_x = \alpha_{He}$$

Same aperture

$$\Delta\Omega_x = \Delta\Omega_{He}$$

Same detector

$$\beta_x = \beta_{He}$$

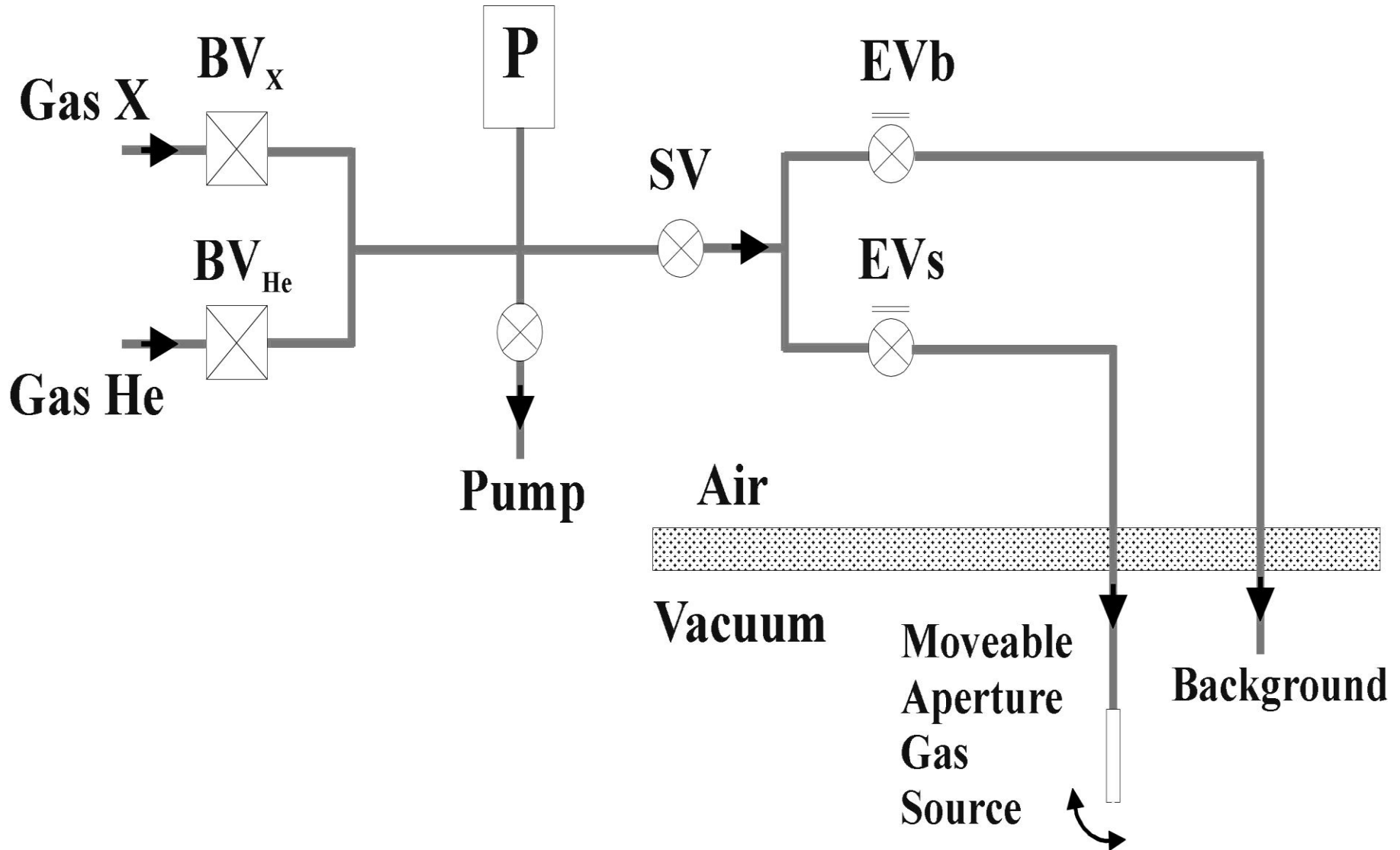
Same system

$$I_s^x = I_o^x \dot{P}_x \sqrt{m_x} \frac{d\sigma_x}{d\Omega}$$

$$I_s^{He} = I_o^{He} \dot{P}_{He} \sqrt{m_{He}} \frac{d\sigma_{He}}{d\Omega}$$

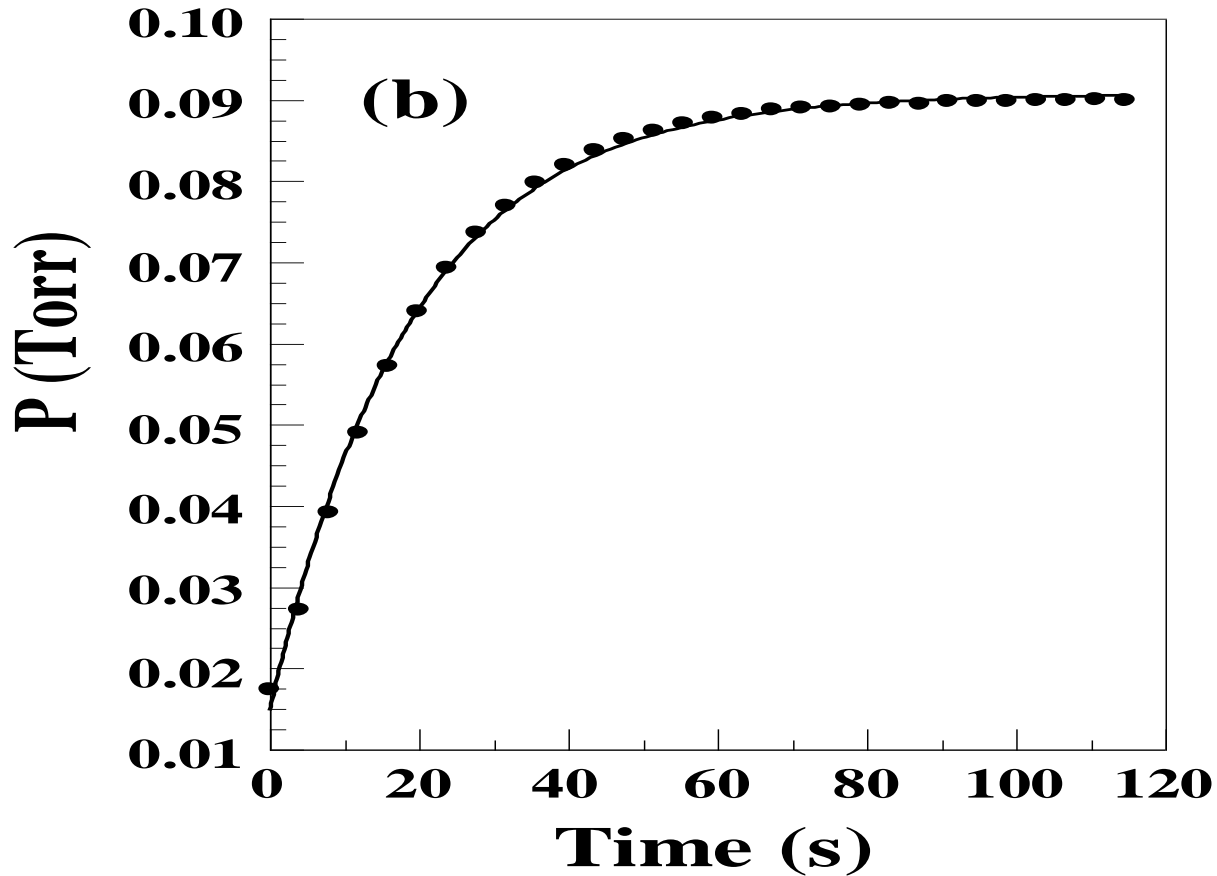
$$DCS_x (E_o, \theta) = \frac{I_s^x I_o^{He} \dot{P}_{He} \sqrt{m_{He}}}{I_s^{He} I_o^x \dot{P}_x \sqrt{m_x}} DCS_{He} (E_o, \theta)$$

# Measuring the Flow Rate

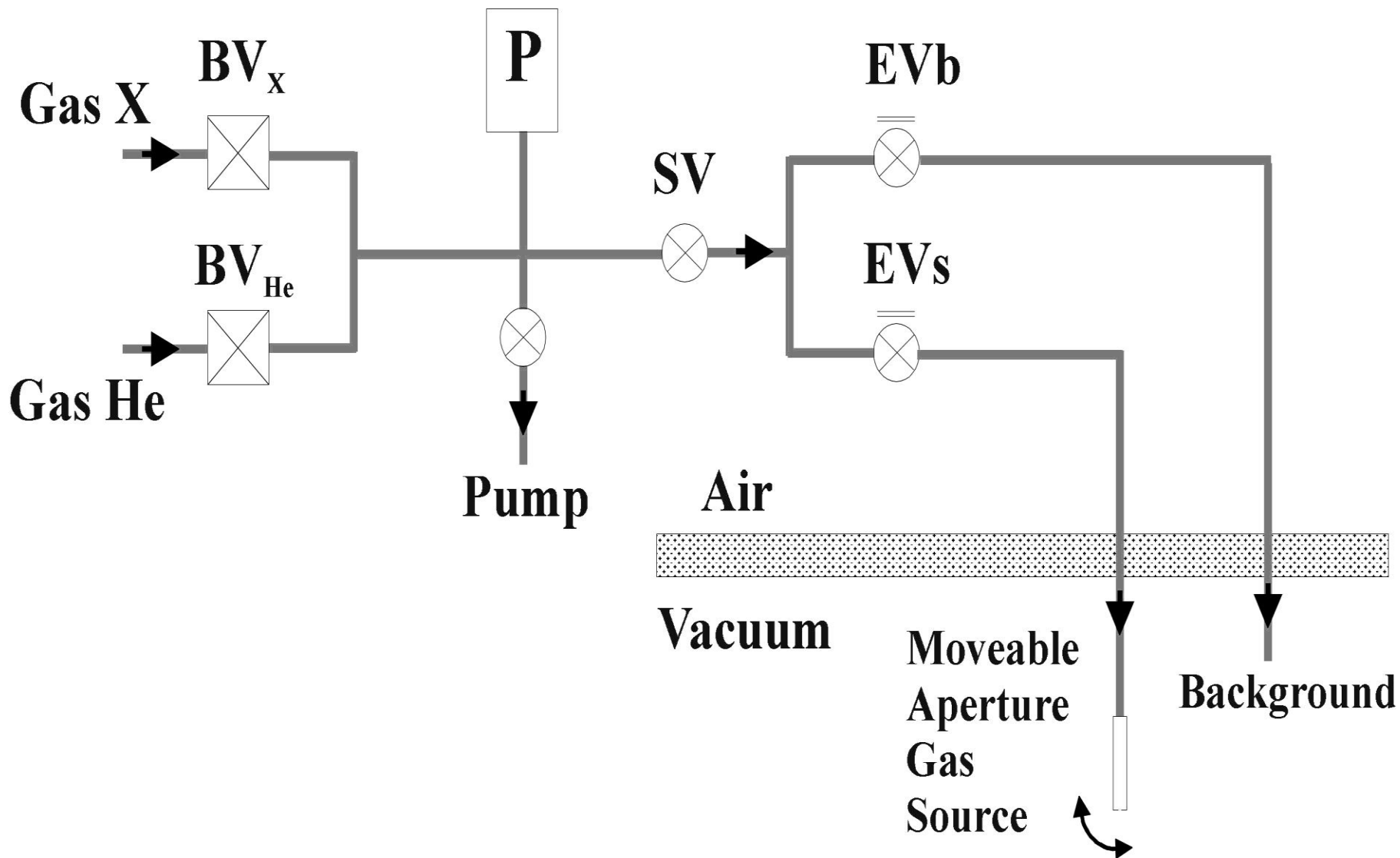


# Stabilization Through Aperture

## P measurements

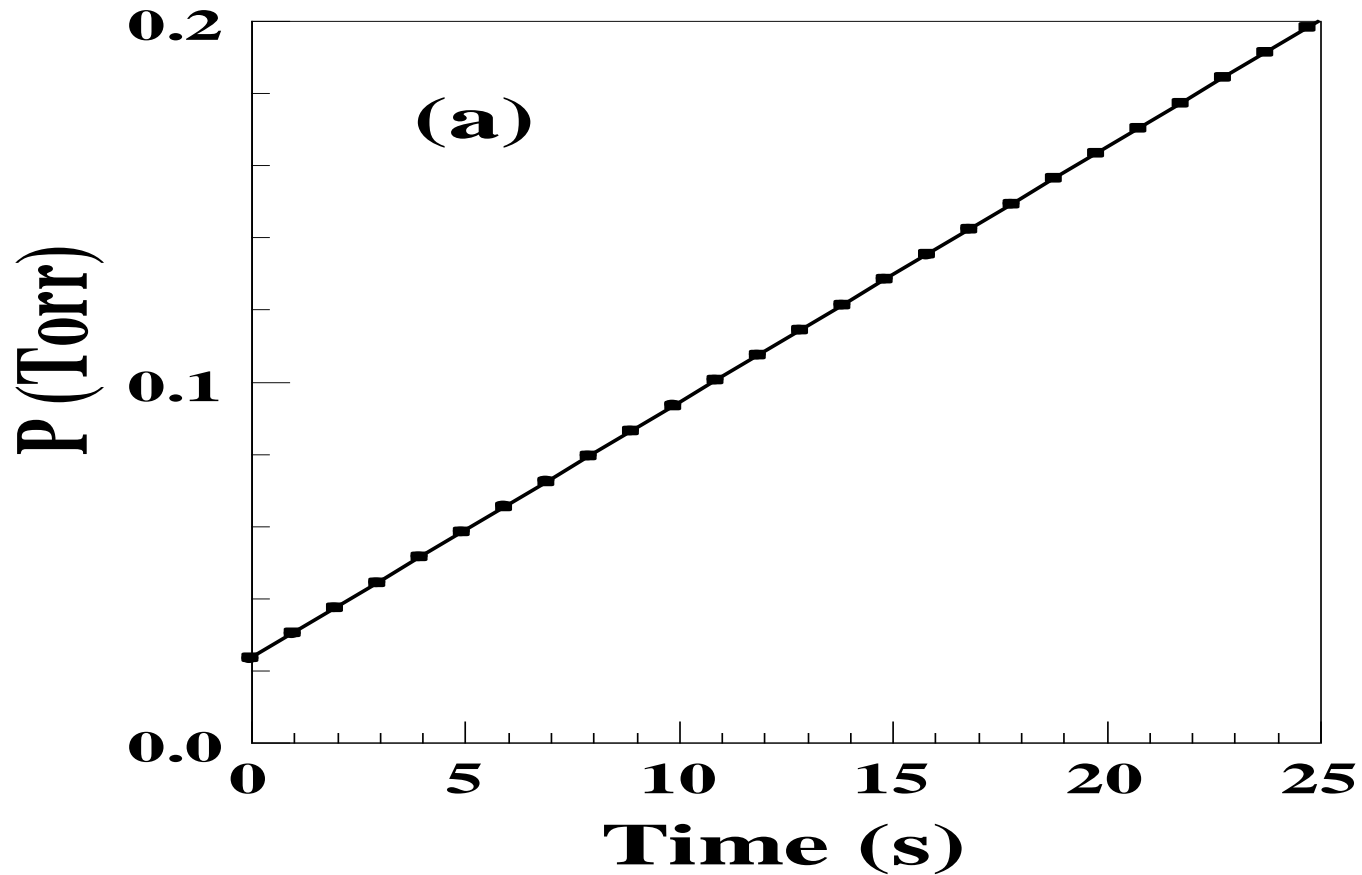




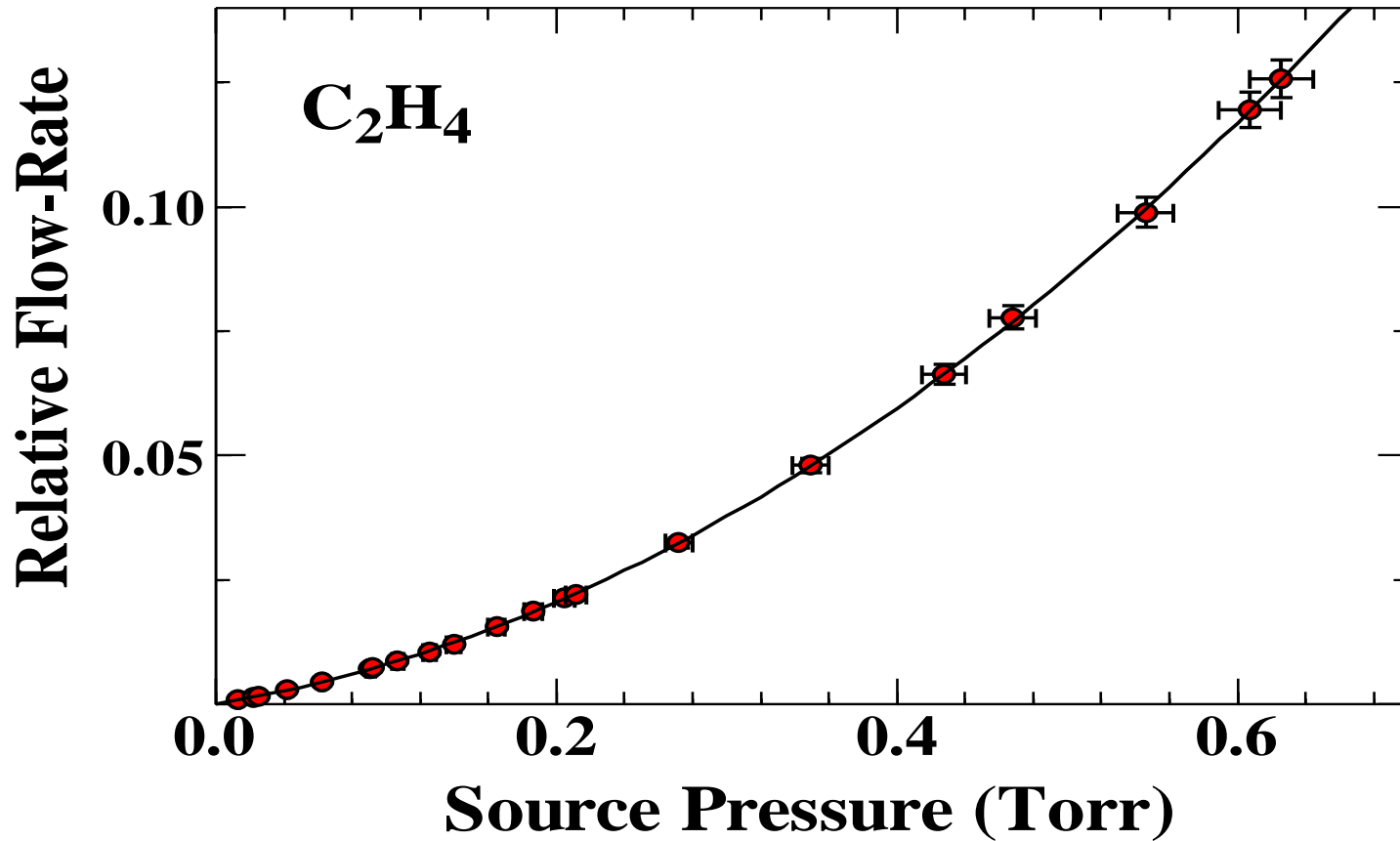


# Filling of Evacuated Volume

## $dP/dt$ measurements



# dP/dt vs. P

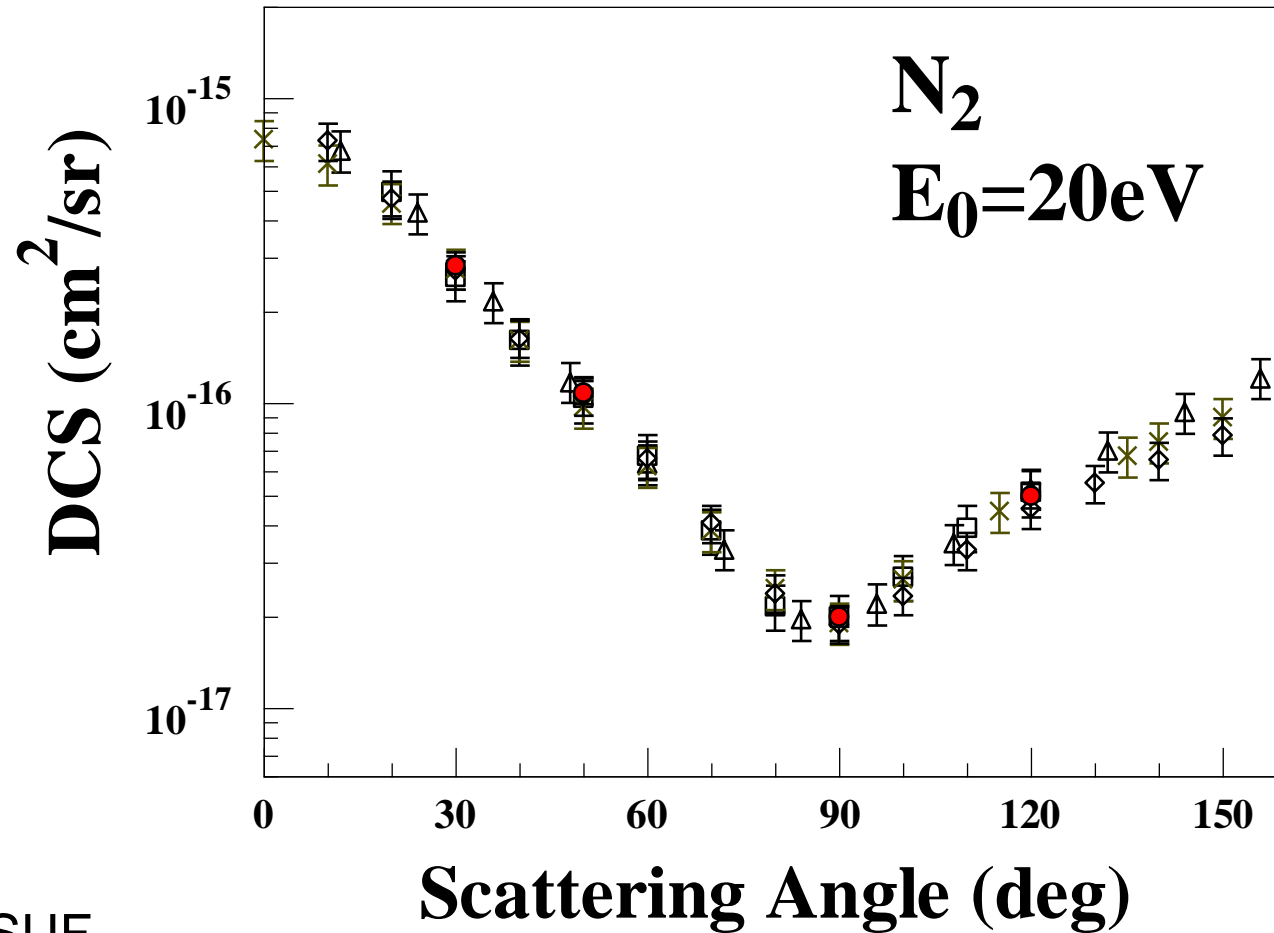


# Initial Tests with a Known Gas - N<sub>2</sub>

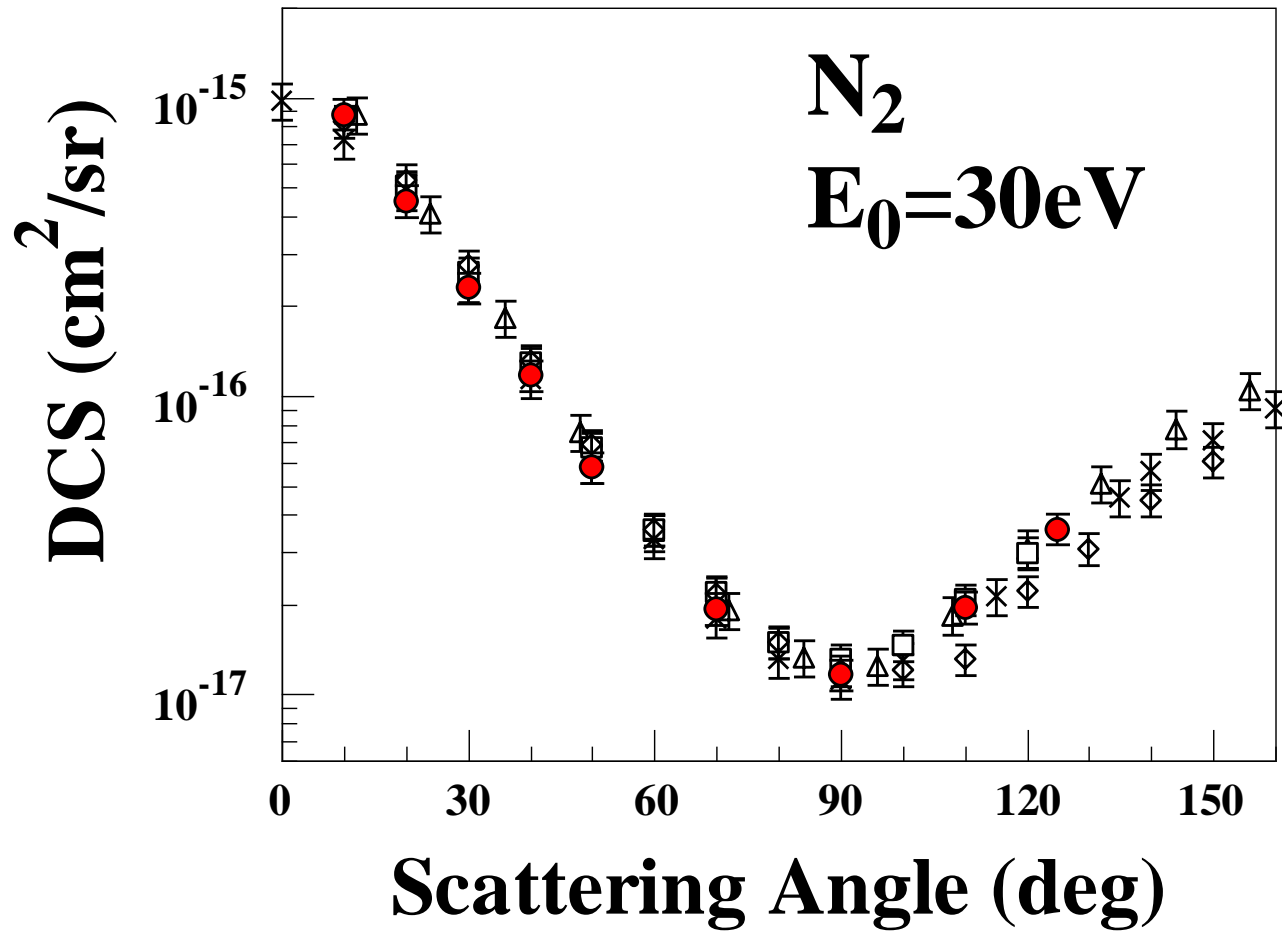
## DCSs available:

- × Srivastava et al., JPL, CA
- △ Shyn and Carignan, Ann Arbor, MI
- Nickel et al., UC Riverside
- ◇ Gote and Ehrhardt, Kaiserslautern, GE

# Molecular Nitrogen at 20eV



# Molecular Nitrogen at 30eV



● CSUF

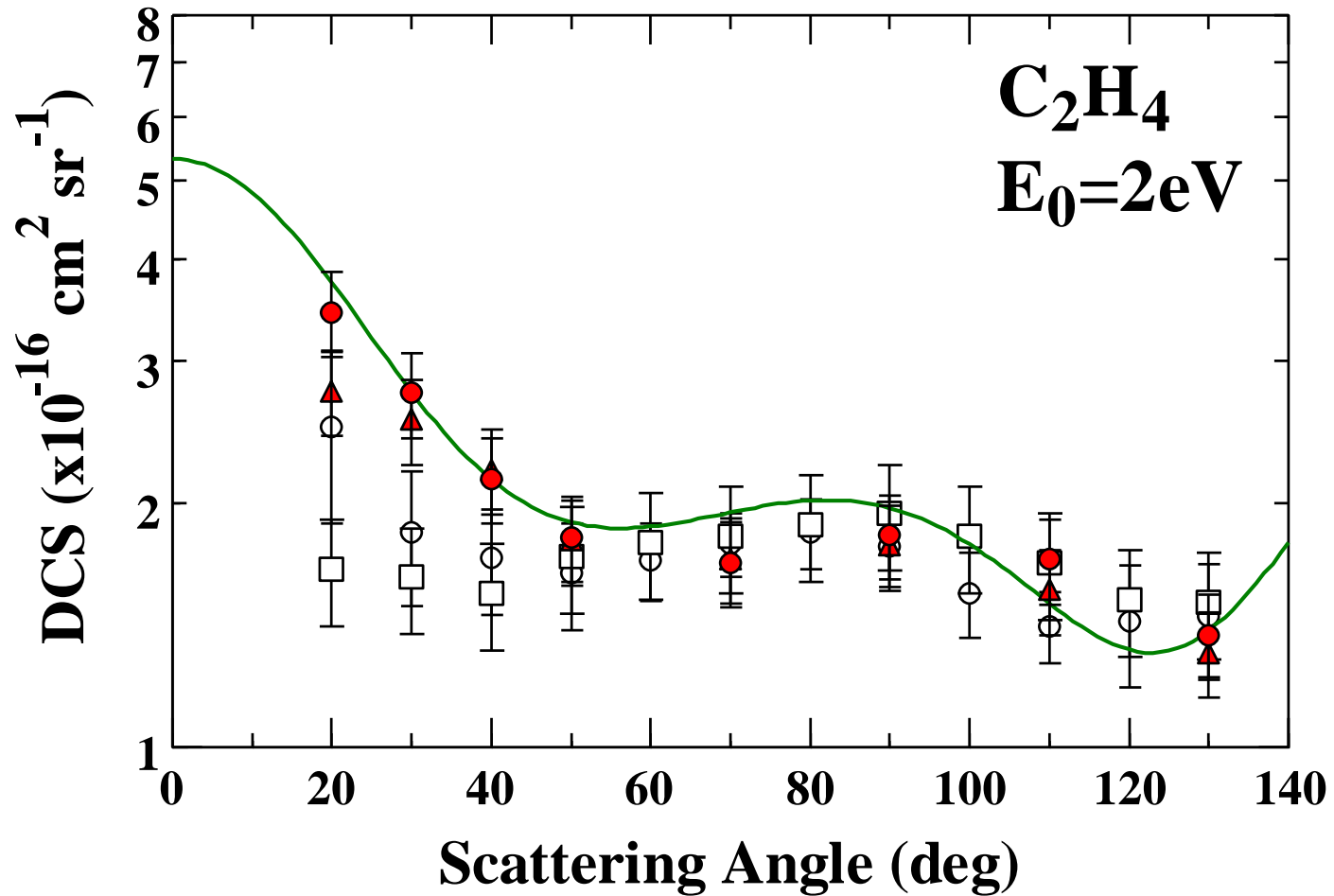
## Final Results:

Differential Cross Sections:

Ethylene at

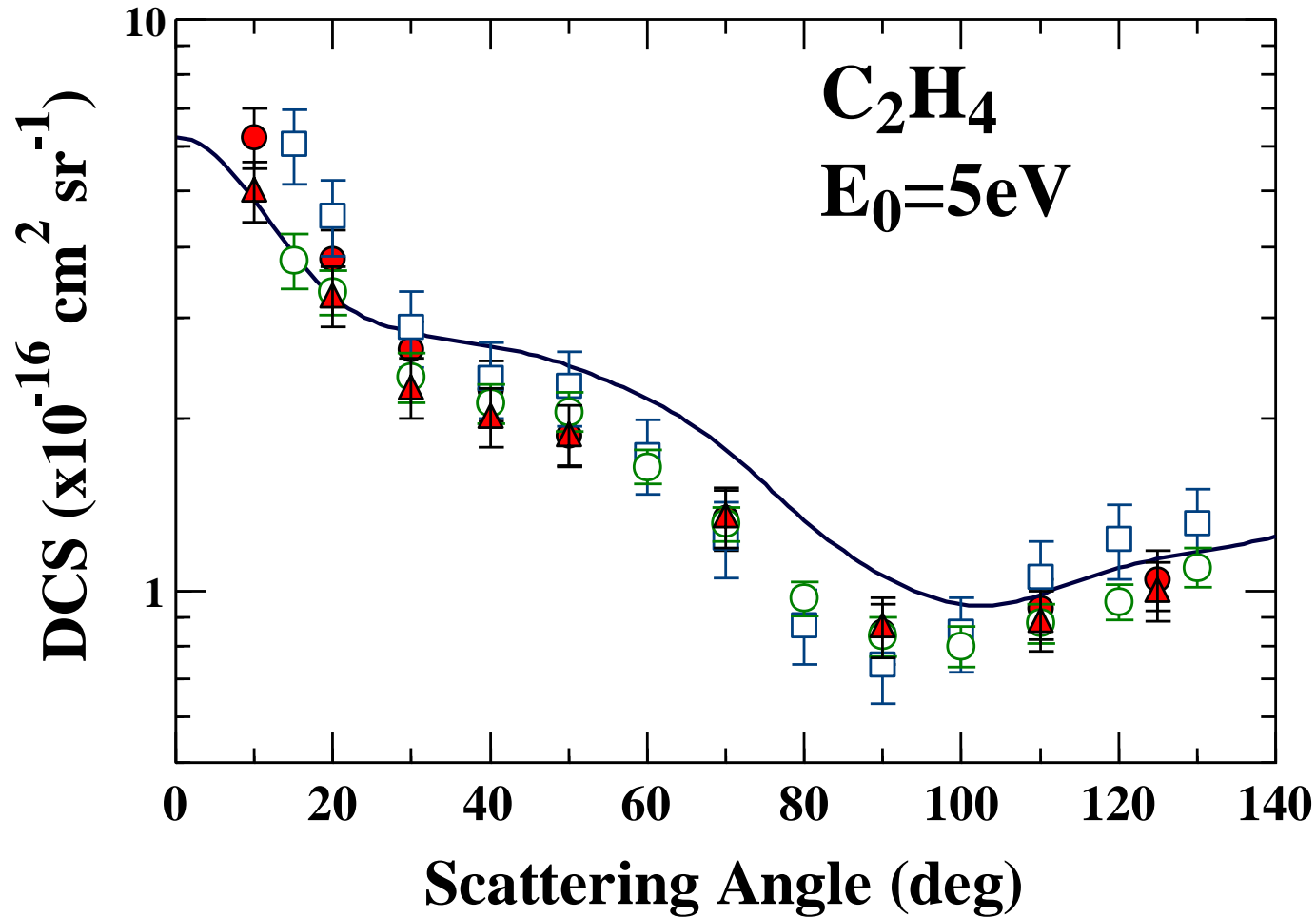
Incident energies of

2eV, 5eV, 10eV, 20eV, and 30eV

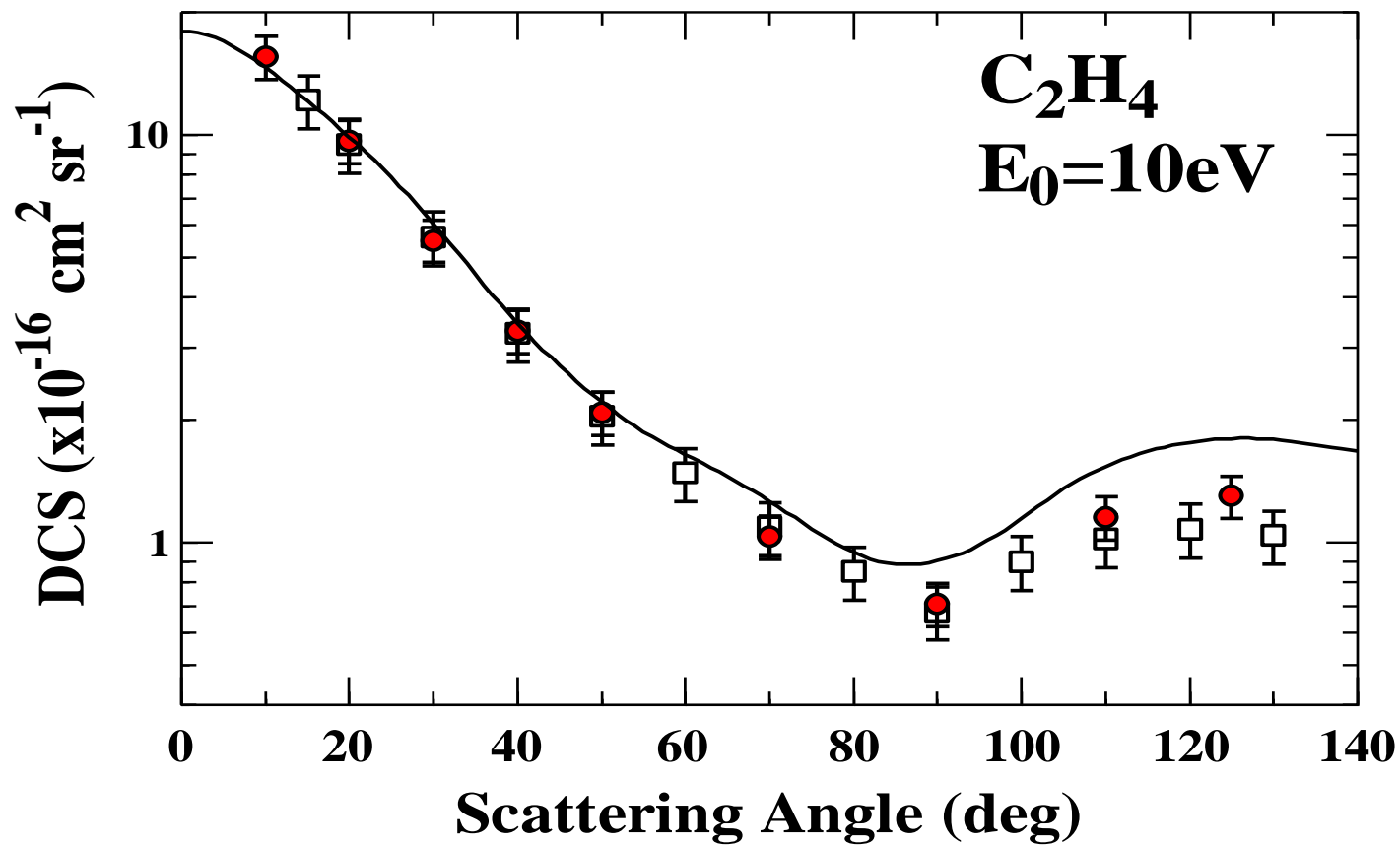


- ● CSUF    ▲ CSUF 4-5 days later requiring a retune of spectrometer
- ○ ANU Data    □ Sophia U.
- — Caltech Theory

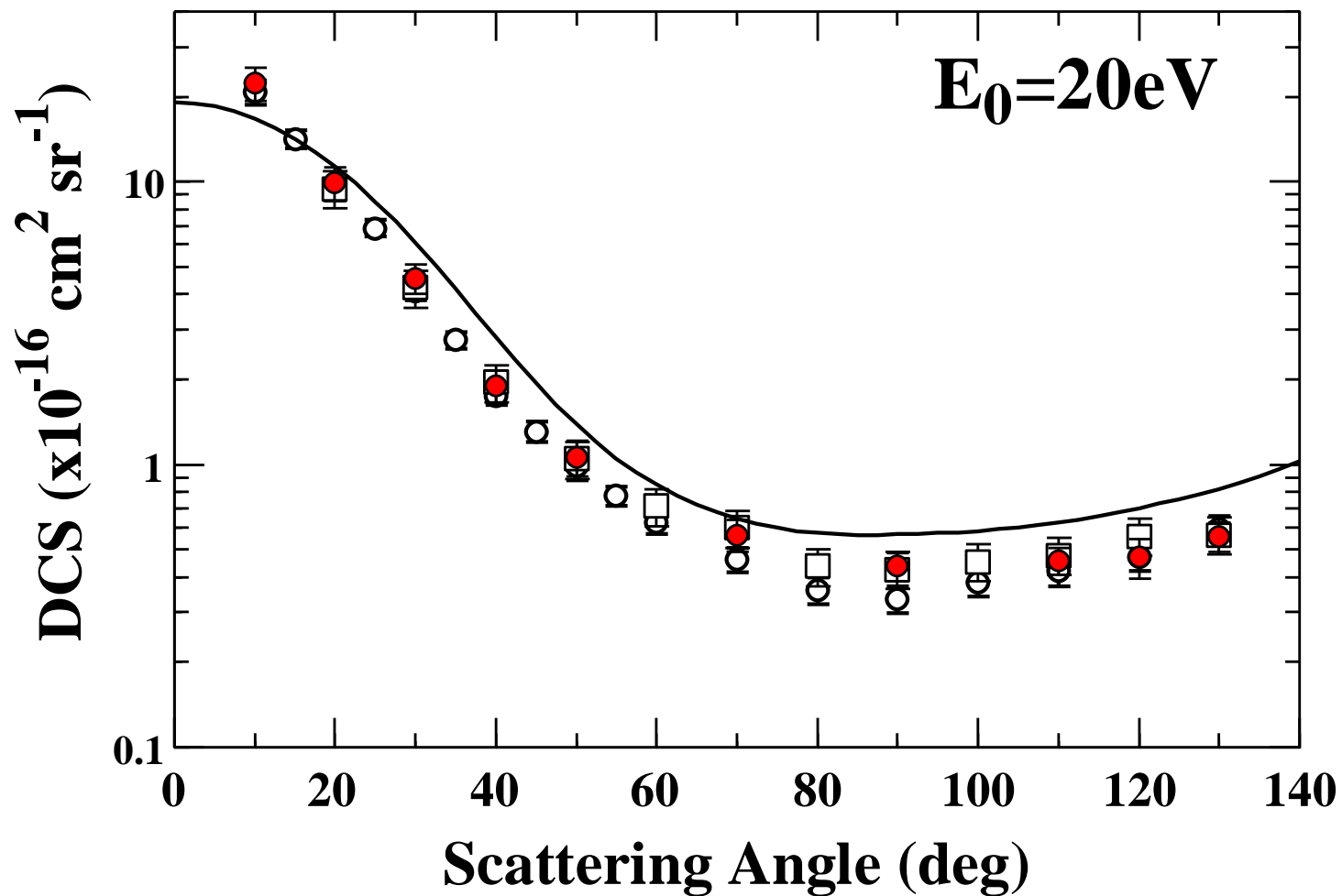




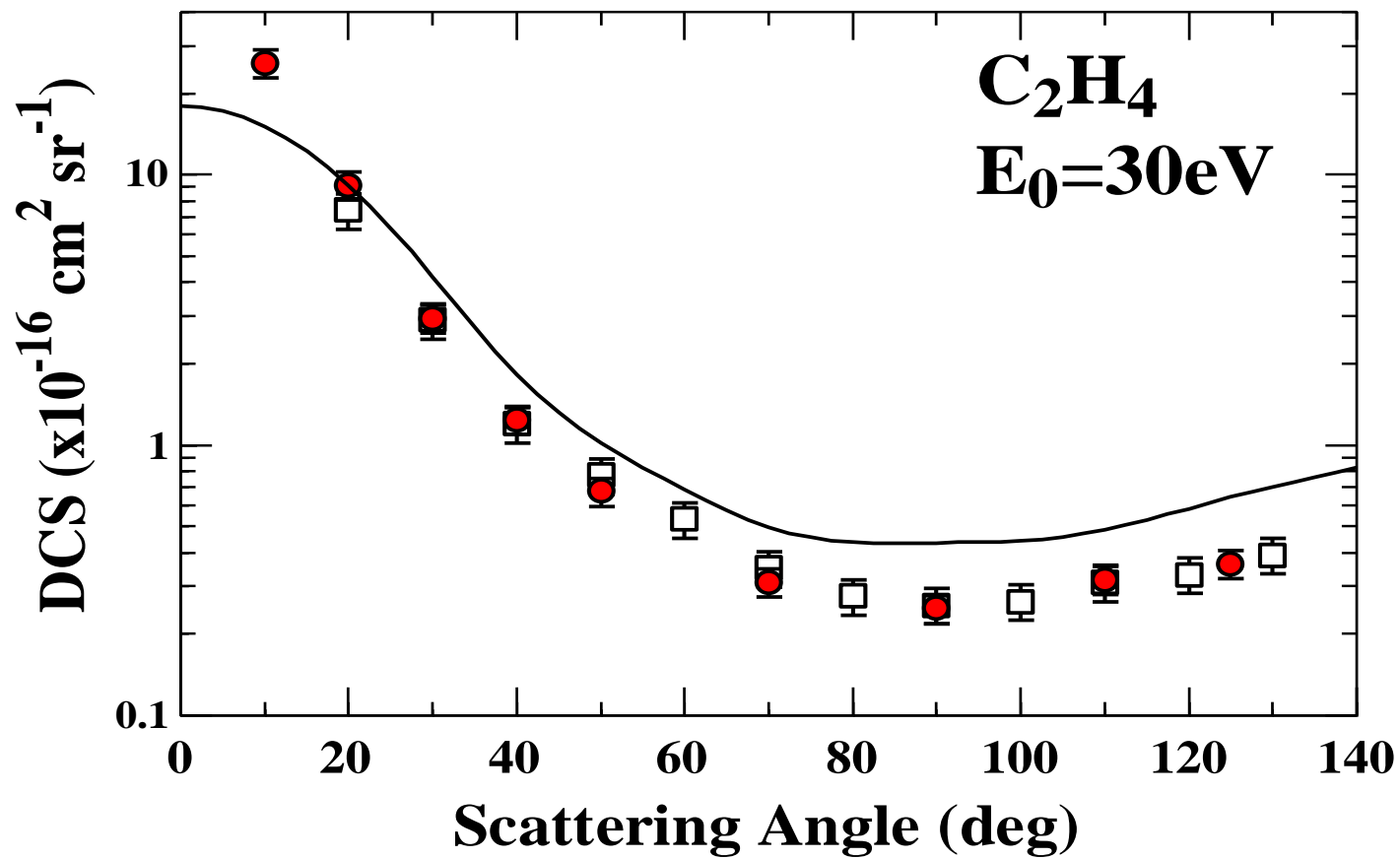
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- ● CSUF
- ○ ANU Data    □ Sophia U
- — Caltech Theory

# Conclusions

- $C_2H_4$  expts are on solid ground
- Our method clearly works
- Simple to apply
- Rapid and reliable
- Does not need to know  $\delta$  for the target gas and can therefore be extended to molecules whose  $\delta$ -values are unavailable  
e.g.  $CH_3OH$ ,  $C_2H_5OH$ ,  $C_3H_7OH$ ,  $H_2O$  (?),  
Bio-molecules

Presently have extended technique  
to  $\text{CH}_3\text{OH}$  and  $\text{C}_2\text{H}_5\text{OH}$

**Poster R1.00099**

An Accurate, but Novel Application of the Relative Flow  
Technique, Using a Moveable Aperture Source of Gas  
Atoms to Measure Elastic Electron Scattering Differential  
Cross Sections

TELUS Convention Centre - Exhibition Hall B

**Friday 4:00pm - 6:00pm**